




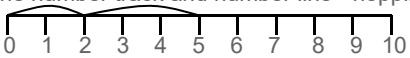




Progression in Addition

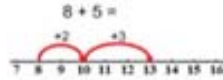
National Curriculum 2014

Year	What will addition look like?	Guidance
EYFS	<p>Practical, counting objects and relating addition to combining two groups of objects</p> <p>Nursery Count on in familiar and practical contexts Songs, rhymes and stories: 1,2,3,4,5 once I caught a fish alive...</p>  <p>Relate addition to combining two groups of objects</p> <p>3 and 2 more is 5</p>  <p>Reception Put biggest number first and count on. Using numbers on a washing line or jumping along a number track</p>  <p>Use a number track to count on.</p> <p>Begin to use + and = sign to record mental calculations in a number sentence.</p>  <p>Using Numicon to support Addition</p> <p>If using Numicon, children could use printed Numicon icons and stick these in - progressing to recording number sentences alongside</p>  <p>1 + 2 = 3</p>	<p>The guidance in italics is taken from the non-statutory guidance in the 'National Curriculum in England' document for 2014</p>
1	<p>Use of the number track and number line - hopping and recording.</p> <p>(a)  2 and 3 equals 5</p> <p>$2 + 3 = \square$ $5 + 3 + 1 = 9$</p> <p>$\square + \triangle = 4$</p> <p>$10 = 6 + \triangle$</p> <p>Continue to develop pupils' understanding of addition with practical activities using concrete apparatus, such as bundles of straws, numicon, counters and diennes.</p>	<p><i>Pupils memorise and reason with number bonds to 10 and 20 in several forms (e.g. $9 + 7 = 16$; $16 - 7 = 9$; $7 = 16 - 9$). They should realise the effect of adding or subtracting zero. This establishes addition and subtraction as related operations.</i></p> <p><i>Pupils combine and increase numbers, counting forwards and backwards.</i></p> <p><i>They discuss and solve problems in familiar practical contexts, including using quantities. Problems should include the terms put together, add, altogether, total, take away, distance between, more than and less than, so that pupils develop the concept of addition and subtraction and are enabled to use these operations flexibly.</i></p>

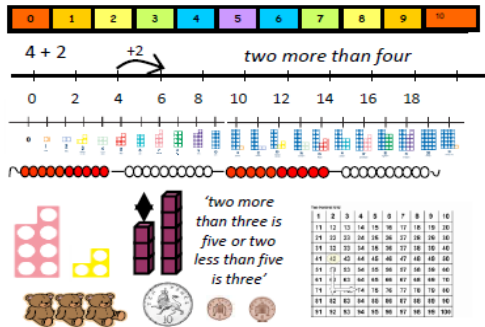
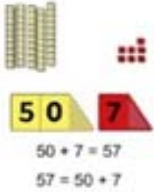
Number lines to add units



Begin to use number lines to bridge across 10 to solve additions



Partition numbers and write the addition using + and =, using dienes and place value arrows



Use practical resources such as bears, counters, cubes and number lines/hundred grids and progress to a resource such as Numicon to encourage counting in groups rather than ones

FLUENCY

Count forwards, to and across 100, beginning with 0 or 1 or from any given number.

Switch count between tens and ones e.g. 10, 20, 30, 31, 32, 33 ...

Represent and use number bonds up to 20 (establish addition and subtraction as related operations)

Find one more than a number

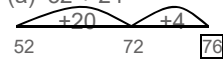
Find ten more than a number

Count in multiples of 2s, 5s and 10s starting on multiples to highlight pattern recognition.

2

Pupils continue to use the number line to calculate with bigger numbers, partitioning the smaller number and adding the most significant digit first

(a) $52 + 24 = \square$ (b) $61 + 14 = \square$



(c) $12 + 7 + 4 = \square$

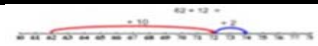
When children have a good understanding of place value and partitioning, introduce the columnar methods with additions that do not cross the tens boundary using concrete apparatus laid out in a columnar form.



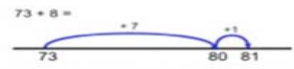
Pupils extend their understanding of the language of addition and subtraction to include sum and difference

Pupils practise addition and subtraction to 20 to become increasingly fluent in deriving facts such as using $3 + 7 = 10$, $10 - 7 = 3$ and $7 = 10 - 3$ to calculate $30 + 70 = 100$, $100 - 70 = 30$ and $70 = 100 - 30$. They check their calculations, including by adding to check subtraction and adding numbers in a different order to check addition (e.g. $5 + 2 + 1 = 1 + 5 + 2 = 1 + 2 + 5$). This establishes commutativity and associativity of addition.

Recording addition and subtraction in columns supports place value and prepares for formal written methods with larger numbers.



Children use empty number lines to add tens and units. They use these to bridge through multiples of 10 using their number bond knowledge

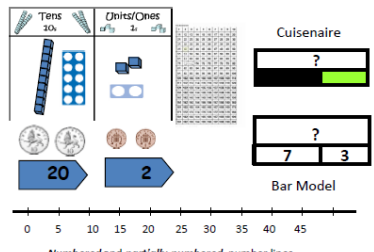
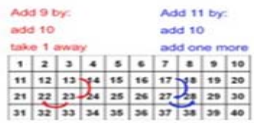


Children begin to partition two digit numbers horizontally and then begin to add tens and units vertically

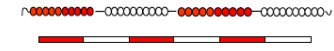
$$\begin{array}{r} 37 + 22 = \\ 30 + 7 \\ 20 + 2 \\ \hline 50 + 9 = 59 \end{array}$$

Children use a number square to add 10 and multiples of 10.

Children begin to use a number square to add 9 and 11.



Numbered and partially numbered number lines



Use Numicon, number grids, place value apparatus/Dienes, place value grids, place value cards. Encourage children to partition numbers rather than counting in ones.

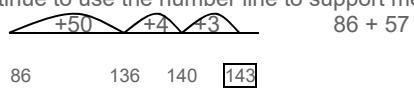
FLUENCY

Show increasing fluency in deriving pairs of numbers up to 10 and then up to 20.

Use knowledge to derive and use number facts up to 100.

Add numbers mentally including TO + U, TO + tens, TO + TO, O + O + O.

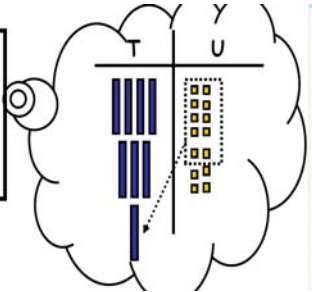
(a) Pupils continue to use the number line to support mental calculation



3 Pupils build on their understanding of place value, partitioning and their concrete experiences to develop columnar methods of addition which bridge the tens, then hundreds, initially in the expanded form.

Expanded method
It is important that the children have a good understanding of place value and partitioning using concrete resources and visual images to support calculations. The expanded method enables children to see what happens to numbers in the standard written method.

$$48 + 36$$



$$\begin{array}{r} 60 + 7 \\ 20 + 4 \\ 10 \\ 90 + 1 = 91 \end{array}$$

and check answer using the inverse

Progressing to 3 digit numbers

124+

Pupils practise solving varied addition and subtraction questions. For mental calculations with two-digit numbers, the answers could exceed 100.

Pupils use their understanding of place value and partitioning, and practise using columnar addition and subtraction with increasingly large numbers up to three digits to become fluent

137
 11(ones)
 50 (tens)
 200 (hundreds)
 261

and check answer using the inverse

Children to be confident using the practical apparatus to support if necessary.

The resources shown include:

- A 100 grid with numbers 1 to 100.
- Base ten blocks representing 100s, 10s, and 1s.
- Cuisenaire rods representing 100s, 10s, and 1s.
- A number line from 0 to 50.
- Partially numbered and blank number lines.
- A Cuisenaire bar model with a question mark and a green rod.
- A Bar Model with a question mark and two boxes labeled 70 and 30.

Fluency

Count in ones, tens and hundreds maintaining fluency through varied and frequent practice

Count from 0 in multiples of 4,8,50 and 100

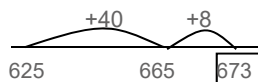
Find 10 or 100 more than a number
 Mentally add HTO + O, HTO + tens, HTO + hundreds

Perform mental calculations with two-digit numbers, the answer could exceed 100

4

Partition one number when adding **mentally**

(a) $625 + 48 =$

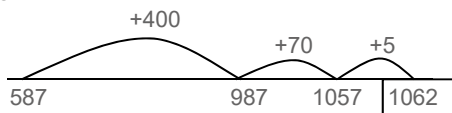


Pupils use their understanding of the expanded columnar methods of addition to progress to use the compact method.

$$\begin{array}{r} 625 + \\ 48 \\ \hline 673 \\ 1 \end{array}$$

$$\begin{array}{r} 1294 + \\ 2345 \\ 3639 \\ \hline 1 \end{array}$$

Adding larger numbers mentally, partitioning the smaller number
 $587 + 475 =$



Pupils use the compact column method to calculate with decimal numbers, and with larger whole numbers.

$$\begin{array}{r} \text{£ } 6.72 + \\ 8.56 \end{array}$$

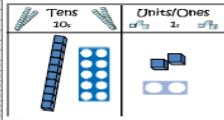
Pupils continue to practise both mental methods and columnar spacing addition and subtraction with increasingly large numbers to aid fluency.

Pupils practise using the formal written methods of columnar addition and subtraction with increasingly large numbers to aid fluency. They practise mental calculations with increasingly large numbers to aid fluency.

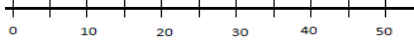
+ 2.30
£ 17.58

Children to be confident using the practical apparatus to support if necessary.

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100
101	102	103	104	105	106	107	108	109	110
111	112	113	114	115	116	117	118	119	120
121	122	123	124	125	126	127	128	129	130
131	132	133	134	135	136	137	138	139	140
141	142	143	144	145	146	147	148	149	150
151	152	153	154	155	156	157	158	159	160
161	162	163	164	165	166	167	168	169	170
171	172	173	174	175	176	177	178	179	180
181	182	183	184	185	186	187	188	189	190
191	192	193	194	195	196	197	198	199	200



Hundreds 100s	Tens 10s	Units/Ones 1s



Partially numbered and blank number lines

Cuisenaire	Bar Model

FLUENCY

Count in 6s, 7s, 9s, 25s and 100s

Find 1000 more than a number

Perform mental calculations with increasingly large numbers to aid fluency